

Charge Transfer and Fractional Bonds in Stoichiometric Boron Carbide

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Supporting Information

B oron carbide is one of the most versatile materials of current technological importance.¹⁻³ Low costs of synthesis combined with many useful properties, such as extreme hardness, photocatalytic activity, a high Hugoniot elastic limit, thermoelectricity, *p*-type semiconducting behavior, paramagnetism and high thermal and chemical stability have made boron carbide a preferred material for a variety of technological applications.¹⁻⁷ Despite decades of intense research, the origin of such diverse properties in boron carbide has not yet been fully understood.^{1,2} The major challenge to explain the chemical and physical properties of boron carbide in terms of its crystal structure and chemical bonding has remained an unsolved puzzle.²

Boron carbide crystallizes in the αR -boron⁸ structure type (Figure 1a,b) with $R\overline{3}m$ symmetry, and has the remarkable power to maintain the same general structure through a large variation of atomic proportions.¹⁻³ Single-crystal X-ray diffraction studies^{9–11} have shown that the structure of boron carbide



Figure 1. (a) Crystal structure of $B_{13}C_2$. C atoms are drawn in the color gray; $B_{\rm E}$, $B_{\rm P}$ and $B_{\rm C}$ atoms are drawn in the colors red, blue and green, respectively. The CBC units in $B_{13}C_2$ are drawn with thick bonds. (b) Crystal structures α R-boron with same atom color code as in panel a. Two-electron—three-center (*2e3c*) bonds in α R-boron are shown as red triangles. (c) 6 Å × 6 Å section of the Laplacian in the $B_{\rm P}$ – $B_{\rm P}$ – $B_{\rm p}$ face of the B_{12} cluster in $B_{13}C_2$. Contour lines for the Laplacian are at ±(2, 4, 8) × 10ⁿ eÅ⁻⁵ (-3 ≤ n ≤ 3) intervals. Locations of valence shell charge concentrations (VSCCs) are mentioned. (d) Same as in panel c in the case of α R-boron.

with composition B₁₃C₂ consists of icosahedral B₁₂ clusters and linear CBC chains. The icosahedral unit comprises two crystallographically independent boron atoms, denoted as B_{Polar} and $B_{Equatorial}$ (henceforth, B_{P} and B_{E}). The central boron atom of the CBC chain is denoted as B_{Chain} (henceforth B_C). The B_P atoms of the B_{12} cluster participate in the intercluster B_p-B_p bonds, whereas the B_E atoms are bonded to the C atoms of the CBC chains. In carbon-rich boron carbide with a composition close to $\sim B_{12}C_3$ (i.e., $\sim B_4C$), extra carbon atoms statistically replace the B_P atoms in the B_{12} cluster, ^{1,2,12,13} while maintaining the same basic crystal structure of B₁₃C₂. Using phonon spectroscopy and theoretical calculations, various other atomic combinations, such as B_9C_3 , $B_{10}C_2$ and $B_{11}C$ icosahedra, and CCC, CCB, CBB, BCB, BBB, BVaB (Va means vacancy) and BB₂B chains have also been suggested as possible constituent units of various boron carbide systems.^{1,14-17} Although these studies give a detailed picture of the crystal structures and possible disorders in these systems, they have so far not been able to provide a satisfactory explanation of the chemical bonding and the structure-property relationship in boron carbide.^{2,17}

A quantitative aspherical electron density (ED)¹⁸ study based on high-resolution single-crystal X-ray diffraction data should provide a better understanding of chemical bonding and the structure-property relationship in boron carbide. Recently, we were able to successfully model the ED distribution in stoichiometric $B_{13}C_2$ by multipole (MP) method using the computer program XD2006¹⁹ against an extensive single-crystal synchrotron X-ray diffraction data set.¹¹ The MP model with lattice parameters a = 5.5962(3) Å, c = 12.0661(7) Å yielded an excellent fit to the diffraction data with $R_F(obs) = 0.0197$, $wR_F^2(\text{obs}) = 0.0290$ [obs. criteria: $I > 3\sigma_I$] (see the Supporting Information (SI)). The composition B6.51(12)C measured by energy dispersive X-ray spectroscopy, together with the best fit of the ordered B₁₂CBC model to the extensive single-crystal X-ray diffraction data set, have provided conclusive evidence for the absence of disorder and defects in the crystal (see SI Section S1).¹¹ In the previous report on the synthesis of a defects and disorder free single crystal of $B_{13}C_2$ ¹¹ the basic chemical bonding in $B_{13}C_2$ was assumed to be same as in αR -boron, because both materials possess similar structures (Figure 1a,b). However, a subsequent comparative quantitative analysis of the topological and integrated properties of the experimental EDs in $B_{13}C_2$ and in αR -boron⁸ now reveals a subtle difference (Tables 1, 2, S1–S5, Figure 1c,d, S1–S3).

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Table 1. Bond Distances and Topological Properties of the Experimental Static EDs for $B_{13}C_2$ (ref 11) and in αR -Boron⁸

Bond	d (Å)	$d_{\rm BCP}$ (Å)	$ ho_{\mathrm{CP}} \left(\mathrm{e}/\mathrm{\AA}^3 ight)$	$ abla^2 ho_{\rm CP} ({ m e}/{ m \AA}^5)$						
Intracluster 2c bonds, BCPs										
$(B_P - B_P)_{BC}$	1.8053(4)	0.878/0.932	0.736	-0.556						
$(B_P - B_P)_{\alpha B}$	1.7555(5)	0.890/0.890	0.820	-2.258						
$(B_{P}-B_{E})_{BC}$	1.7997(4)	0.972/0.834	0.761	-1.942						
$(B_P - B_E)_{\alpha B}$	1.8093(5)	0.865/0.946	0.745	-1.388						
$^{\#}(B_{P}-B_{E})_{BC}$	1.7848(5)	0.912/0.874	0.802	-1.675						
$^{\#}(B_{P}-B_{E})_{\alpha B}$	1.8028(3)	0.858/0.945	0.764	-1.950						
$(B_E - B_E)_{BC}$	1.7590(3)	0.886/0.886	0.742	-1.991						
$(B_E - B_E)_{\alpha B}$	1.7868(6)	0.894/0.894	0.804	-2.470						
Intracluster 3c bonds, RCPs										
$(B_{P}-B_{P}-B_{P})_{BC}$			0.651	0.866						
$(B_p - B_p - B_p)_{\alpha B}$			0.795	-1.155						
$(B_{P}-B_{P}-B_{E})_{BC}$			0.700	0.200						
$(B_P - B_P - B_E)_{\alpha B}$			0.704	-1.955						
$(B_{E} - B_{E} - B_{P})_{BC}$			0.711	-0.452						
$(B_E - B_E - B_P)_{\alpha B}$			0.716	-4.321						
Intercluster 2c bonds, BCPs										
$(B_p - B_p)_{BC}$	1.7131(4)	0.857/0.857	1.030	-6.463						
$(B_P - B_P)_{\alpha B}$	1.6734(3)	0.837/0.837	1.104	-9.572						
Bonds involving CBC unit in $B_{13}C_2$, BCPs										
$(C-B_E)_{BC}$	1.6037(2)	1.082/0.523	1.097	-8.289						
$(C-B_C)_{BC}$	1.4324(5)	0.938/0.494	1.556	-8.985						
Intercluster $3c$ bond in αR -boron, RCP										
$(B_E - B_E - B_E)_{\alpha B}$			0.557	-1.063						
-										

^{*a*}*d* is the bond-length and $d_{\rm BCP}$ is the distance between BCP and each of the constituent atoms of the bond. Values for $B_{13}C_2$ and αR -boron are indicated by suffixes $_{\rm BC}$ and $_{\alpha B}$ respectively. Prefixes $^{\$}$ and $^{\#}$ indicate two different intracluster $B_{\rm P}$ – $B_{\rm E}$ bonds.

Table 2. Volumes (V) of Atomic Basins and Bader Charges (q) of Atoms in $B_{13}C_2$ [ref 11] and in αR -Boron⁸ along with Multiplicity (m) in Unit Cell

	B ₁₃ C ₂			aR-boron		
Atom	т	$V(Å^3)$	q (e)	т	$V(Å^3)$	q (e)
Bp	6	7.808	-0.210	6	4.763	0.067
B _E	6	5.176	0.703	6	5.139	-0.067
B _C	1	1.936	2.298			
С	2	14.571	-2.610			

The analysis of the topological properties of EDs has been performed with the aid of Bader's quantum theory of atoms in molecules (QTAIM) approach.^{18,20} According to the QTAIM approach, a bonding between two atoms is indicated by the existence of a bond critical point (BCP), which is a local minimum (saddle point) in the ED along the bond path between the bonded atoms. Similarly, a ring critical point (RCP) indicates the presence of a ring closed by the bond paths of bonded atoms. Furthermore, values of the ED at BCP or RCP ($\rho_{\rm BCP}$ or $\rho_{\rm RCP}$) and its Laplacian ($\nabla^2 \rho_{\rm BCP}$ or $\nabla^2 \rho_{\rm RCP}$) characterize properties of the chemical bonds. For example, a strong covalent bond is indicated by a large value $\rho_{\rm BCP}$ and a large negative value of $\nabla^2 \rho_{\rm BCP}$.

The ED from the MP model exhibits BCPs and RCPs for all bonds in $B_{13}C_2$ (Table 1). The existence of BCPs and RCPs for all intracluster bonds indicates the formation of the B_{12} *closo*cluster in $B_{13}C_2$. It can be seen in Table 1 that ρ_{BCP} and ρ_{RCP} corresponding to 2-center (2c) and 3-center (3c) bonds of the B_{12} cluster in $B_{13}C_2$ have similar values with the comparable bonds in α *R*-boron. This indicates that the bonding in the B₁₂ *closo-*cluster in $B_{13}C_2$ is predominantly covalent, as in αR -boron.⁸ Except for the intracluster $B_p - B_p$ bond, the $\nabla^2 \rho_{BCP}$ of all intracluster 2c bonds have similar values as those observed for αR -boron. The intracluster B_P-B_P bond in B₁₃C₂ has a relatively smaller magnitude of $\nabla^2 \rho_{\rm BCP}$ than in αR -boron. The $\nabla^2 \rho_{\rm RCP}$ corresponding to 3c bonds of the B₁₂ cluster in B₁₃C₂ differ drastically from comparable bonds in αR -boron. The difference is largest for the 3*c* intracluster $B_p-B_p-B_p$ bond. In fact, $\nabla^2 \rho_{RCP}$ corresponding to the 3c intracluster $B_P - B_P - B_P$ bond in $B_{13}C_2$ has a large positive value, whereas the comparable bond in αR boron has a large negative value. A positive value of $\nabla^2 \rho_{\rm RCP}$ for the 3c intracluster $B_p - B_p - B_p$ bond can be interpreted using local form of virial theorem as an indication of high kinetic energy density of the electrons associated with this bond.²⁰ The more delocalized nature of the electrons over the polar region of the icosahedral B_{12} cluster in $B_{13}C_2$ compared to αR -boron is clearly visible in the ED maps (Figures 1c,d, S1–S3).

Among the *exo*-cluster bonds in $B_{13}C_2$ (Table 1), the values of $\nabla^2 \rho_{BCP}$ of $C-B_E$ and $C-B_C$ are almost same, but the ρ_{BCP} of $C-B_E$ has a smaller value than the ρ_{BCP} of $C-B_C$. Large negative values of $\nabla^2 \rho_{BCP}$ characterize both $C-B_E$ and $C-B_C$ in $B_{13}C_2$ as 2-electron-2-center (2e2c) boron-carbon covalent bonds. Comparatively higher value of ρ_{BCP} of $C-B_C$ is probably because of the distribution of valence electrons over a short length due to internal pressure.¹¹ The elevated nature of the electron density over the $C-B_C$ bond path compared to $C-B_E$ bond path is visible in Figure 2a.

Consideration of the topological properties of the ED together with the bond-lengths (Table 1) in $B_{13}C_2$ leads to an assignment of six $2e2c C-B_E$ bonds between the B_{12} cluster and neighboring CBC groups as well as two 2e2c C-B_C bonds for each CBC chain. This leaves only five electrons per formula unit of $B_{13}C_2$ remaining, forcing the system to make on average six equivalent electron-deficient $5/3e2c B_P - B_P$ bonds with the six neighboring clusters of each B₁₂ unit (Figure 2b) (see SI Section S2 for detailed electron counting scheme). The claim of 5/3e2c bonds in the $B_p - B_p$ regions is in agreement with the fact that the bondlength, $\rho_{\rm BCP}$ and $\nabla^2 \rho_{\rm BCP}$ of the intercluster B_P-B_P bonds in B₁₃C₂ have values that are intermediate between those expected for 2e2c and 1e2c intercluster B-B bonds (see SI Section S3).^{8,21} The proposal of electron deficient $B_p - B_p$ intercluster bonds in $B_{13}C_2$ is further supported by the fact that the B_{12} cluster is intrinsically electron deficient^{2,8} and is known to form unusual and electron deficient bonds.²¹ The electron deficient 5/3e2c intercluster $B_p - B_p$ bond in $B_{13}C_2$ can be understood by invoking resonance structures with contributing 1e2c and 2e2c B_P-B_P bonds (Figure 2c). Electrons can thus be redistributed via the delocalized icosahedral B₁₂ cluster to achieve the resonance hybrid 5/3e2c bond in $B_{13}C_2$, somewhat similar to the delocalized π -electron-assisted resonance structure in 2-norbornyl cation.²² From known bond-lengths of 1e2c (1.83 Å) and 2e2c (1.66 Å) bonds,²¹ the bond length of the 5/3e2c resonance hybrid is expected to be close to ~ 1.72 Å, which matches well with the observed value of 1.7131(4).

Despite resonance states, the B_{12} cluster in $B_{13}C_2$ contains on average one unpaired electron, which is responsible for the paramagnetism observed in boron carbide.⁷ The electrondeficient intercluster B_p – B_p bond also explains why in carbonrich boron carbide the B_p atoms of the B_{12} cluster are preferentially replaced by carbon atoms (extra electrons) without affecting the basic crystal structure of $B_{13}C_2$.^{1,2} Similar kinds of electron deficient intercluster bonds might explain why other



Figure 2. (a) Plot of ED along the $C-B_E$ and $C-B_C$ bond paths. The double arrow indicates the region where the ED remains almost constant along the $C-B_E$ bond path. (b) Resonance hybrid 5/3e2c intercluster B_P-B_P bonds. B_P atoms are indicated by open circles. The polar region of the central B_{12} cluster has been marked by elliptical lines. (c) Some of the possible contributing structures for the resonance hybrid 5/3e2c intercluster B_P-B_P bonds. Solid intercluster lines represent 2e2c intercluster B_P-B_P bonds. Solid intercluster lines represent 2e2c intercluster B_P-B_P bonds. A dot is put beside each 1e2c bond in order to indicate that they contain single electron. (d) Laplacian of the static ED in the plane containing the atoms B_E , C and B_C [adapted from Figure 2(f) in ref 11]. Contour lines at $\pm(2, 4, 8) \times 10^n$ eÅ⁻³ ($-3 \le n \le 3$). (e) Schematic representation of charge transfer from the 2p orbitals of the atom B_C to the atom B_P ; only one possible charge transfer is shown for clarity.

compounds related to boron carbide such as boron subarsenide (B₁₂As₂, intercluster bond-length is ~1.77 Å), boron subphosphide (B₁₂P₂, intercluster bond-length is ~1.74 Å) can maintain the same general crystal structure over a range of compositions.¹³ However, presence of unpaired electrons in B₁₃C₂ raises the question as to why B₁₃C₂ is chemically stable? The plausible answer is the lack of a possible pathway. Likely causes are steric hindrance and delocalization of the unpaired electrons; both are known to increase the stability of radicals.^{23,24} Because of the large number of possible contributing structures (Figure 2c), unpaired electrons in B₁₃C₂ are delocalized over a large area, at the same time they are shielded by bulky icosahedral clusters with fully occupied orbitals on their surfaces. These two factors together may make B₁₃C₂ a stable radical. In technical

boron carbide, the chemical stability may further be increased by the presence of electron-releasing impurities such as carbon. Nevertheless, boron carbide should be highly reactive at high temperature, when available unpaired electrons might gain sufficient energy to overcome the shielding effect. Evidence of high reactivity of boron carbide at elevated temperature has recently been discovered.²⁵

From the integrated properties of the electron densities (Table 2), it is found that the volumes of the B_E atomic basins in $B_{13}C_2$ and in α R-boron are almost same, whereas volume of the B_P atomic basin in $B_{13}C_2$ is larger than the same in αR -boron. A large volume of the B_P atomic basin in $B_{13}C_2$ indicates charge accumulation in the B_p atomic basin. Integrated properties of the ED show that different atoms in $B_{13}C_2$ are differently charged. An analysis of the ED distribution along the $C-B_E$ bond-path shows that there exists a length of ~0.20 Å where the ED is almost constant (Figure 2a). Because of this feature, positions of the BCP and the zero-flux surface^{18,20} between the atom C and the atom B_E are dependent on minor variations of the experimental data and thus poorly determinable. Considering this uncertainty as well as the fact that carbon is more electronegative than boron, it can be understood from Table 2 that most part of the large negative charge of the atom C is probably contributed by the three bonded B_E atoms, whereas B_C atom probably contributes a minor part. However, uncertainties in partitioning and the difference between electro-negativities of carbon and boron together cannot alone explain large positive charge of 2.298 e of the atom B_C . The large positive charge of the atom B_C thus indicates absence of electrons at the B_C site.

Absence of valence shell charge concentrations in the electron density at the position of the 2p orbitals oriented perpendicularly to the CBC unit (Figure 2d) indicates that these orbitals of the atom B_C are empty. A very small volume of the B_C atomic basin indicates that the atom B_C gives away its 2p electron. In contrast, it should be noted that the volume of the B_P atomic basin is relatively large and the atom $B_{\rm p}$ is slightly negatively charged. Because the distribution of ED along the intercluster B_P-B_P bond path is crystallographically symmetric and because there is no difference in electro-negativities between the atom B_P and its neighbors, it is unlikely that there is a buildup of negative charge on the atom B_p unless some charge transfer is taking place. The negative electronic charge of the atom B_p thus indicates that a charge transfer from the atom B_C to the atom B_P occurs. Because the 2p orbitals of the atom B_C are empty, it is most likely that the electron is transferred from these orbitals (Figure 2e). The observation of *p*-type excitons at the B_C site in boron carbide²⁶ supports the claim of the charge-transfer from the 2p orbitals of the atom B_{C} . It is to be expected that transfer of an electron from B_{C} will be equally distributed over all 6 equivalent B_{P} atoms of the B₁₂ cluster. If this occurs, each B_P atom should have on average a negative charge of $\sim 1/6e$, which approximately matches with the Bader charge of the B_P atom (-0.210 *e*). This view is supported by the shape of the B_{12} icosahedron, which is elongated along the crystallographic 3-fold axis of symmetry such that the distances of the B_P atoms to the centroid of the B_{12} icosahedron at 1.725 Å are significantly longer than those of the B_E atoms (1.679 Å). Observations of photocatalytic activity,⁵ Seebeck effect⁶ and *p*type excitons²⁶ in boron carbide suggest that the transfer of charge between the atoms $B_{\rm C}$ and $B_{\rm P}$ may occur in both thermal and photo excitations.

In summary, discovery of a new electron-deficient 5/3e2c intericosahedral B–B bond in stoichiometric boron carbide (B₁₂CBC, with $R\overline{3}m$ symmetry) has been reported. It is proposed

that the 5/3e2c bond is caused by a resonance mechanism with contributing 1e2c and 2e2c B–B intericosahedral bonds. The proposed bonding model is consistent with the chemical and physical properties of boron carbide and explains why boron carbide and related materials can preserve the same crystal structure over a range of compositions. This study resolves the long-standing enigma of chemical bonding in boron carbide, and indicates that the properties of boron carbide can be tuned by adjusting the amount of external excitation energy or by changing the chemical composition by bearing the charge distribution in mind. This understanding should have a major impact on designing boron carbide and related materials with improved performance.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.chemma-ter.7b02825.

Details of the MP models and the investigations on possible disorder in $B_{13}C_2$; electron counting scheme; summary of the supporting experimental results, comparison of electron density distributions in $B_{13}C_2$ and αR -boron (Figures S1–S3); crystallographic data and parameters from the MP models of $B_{13}C_2$ and αR -boron (Tables S1–S5) and analysis of possible disorder (Table S6) (PDF)

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Notes

The author declares no competing financial interest.

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